Unit B5: Supplemental Notes, 10/7/03

Note: This applies only to Section 1 (i.e., the 9:30 a.m. class), in which I had trouble explaining one problem of a group exercise.

In-Class Group Exercise

Determine whether the following wff is tautology (always true), contradiction (always false), or neither:

B2: $(\neg p \lor q) \lor (p \lor \neg q)$

Answer:

(a) A conservative, but tedious way to analyze this is to check all the four truth assignments for the propositional variables. This should show that the wff is a tautology.

(b) A simpler way to show that the wff is a tautology is as follows. The formula can be rewritten as $(p \rightarrow q) \lor (q \rightarrow p)$, by applying the equivalence $\neg X \lor Y \Leftrightarrow X \rightarrow Y$ and $X \lor Y \Leftrightarrow Y \lor X$. Then, in order for the entire wff to be false, at least one of $p \rightarrow q$ and $q \rightarrow p$ must be false. The only way to make $p \rightarrow q$ false is to set $p = \mathbf{T}$ and $q = \mathbf{F}$. However, this will make $q \rightarrow p$ true. Thus, the wff cannot be false.

<End>